

Basic Number Properties of Addition

Commutative property of addition: When two numbers are added, the sum is the same regardless of the order of addition. For example: $5 + 4 = 4 + 5$

Associative property of addition: When three or more numbers are added, the sum is the same regardless of the order of addition. For example: $(3 + 4) + 6 = 3 + (4 + 6)$

Example 1

What property is expressed in the following equation?

$$39 + 66 = 66 + 39$$

Explanation

We are **interchanging** two numbers, therefore commutative property is shown.

Example 2

What property is expressed in the following equation?

$$146 + 138 + 54 = 138 + (146 + 54)$$

Explanation

First $146 + 138 + 54 = 138 + 146 + 54$, we are interchanging two numbers, therefore commutative property is applied.

Second $138 + 146 + 54 = 138 + (146 + 54)$, to simplify the calculation, we are re-grouping the numbers of the problem; therefore it is the associative property being applied.

Example 3

Fill in the missing number according to the associative property of addition.

$$213 + 39 + 61 = 213 + (\underline{\quad} + \underline{\quad})$$

Explanation

$$213 + 39 + 61 = 213 + (39 + 61)$$

We are **regrouping the numbers** in the problem and **the sum is same regardless**. Therefore associative property is applied.

Example 4

Use the number properties to simplify the calculation: $147 + 316 + 353$

Explanation

Adding 147 and 353 would yield a number that is multiple of 100. Therefore we apply the **associative property** to group them together.

$$\begin{aligned} & 147 + 316 + 353 \\ = & 147 + 353 + 316 \\ = & 500 + 316 \\ = & 816 \end{aligned}$$

Example 5

Use the number properties to solve: $48 + 158 + 42 + 152$

Explanation

When we look at the patterns of the 4 numbers, they add up to equal 200 if we regroup them.

$$48 + 158 + 42 + 152$$

If we can **regroup** numbers resulting multiple of 10, 100, etc, that would simplify the calculation.



$$\begin{aligned} & 48 + 158 + 42 + 152 \\ = & 48 + 152 + 42 + 158 \\ = & (48 + 152) + (42 + 158) \\ = & 200 + 200 \\ = & 400 \end{aligned}$$

Commutative property is applied.

Associative property is applied.

Strategies involved with subtraction:

Regrouping subtrahends, the difference remains the same: $a - b - c = a - c - b$

Subtracting two numbers is equal to subtracting the sum of two: $a - b - c = a - (c + b)$

Example 6

Solve: $456 - 249 - 156$

Explanation

$$\begin{aligned} & 456 - 249 - 156 \\ &= 456 - \mathbf{156} - \mathbf{249} \\ &= 300 - 249 \\ &= 51 \end{aligned}$$

Example 7

Solve: $397 - 154 - 46$

Explanation

$$\begin{aligned} & 397 - 154 - 46 \\ &= 397 - \mathbf{(154 + 46)} \\ &= 397 - 200 \\ &= 197 \end{aligned}$$